



# Categories and General Algebraic Structures with Applications

Volume 8, Number 1, January 2018  
ISSN Print: 2345-5853 Online: 2345-5861



Shahid Beheshti University  
<http://www.cgasa.ir>

In the Name of God

# Categories and General Algebraic Structures

## with Applications

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**Publisher:** Shahid Beheshti University.



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